# On the Complexity and Typology of Inflectional Morphological Systems

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### What's your native language?





# Do you think your native language more complex than English?





#### Audience Poll

**Question:** Who thinks their native language is more complex than English?

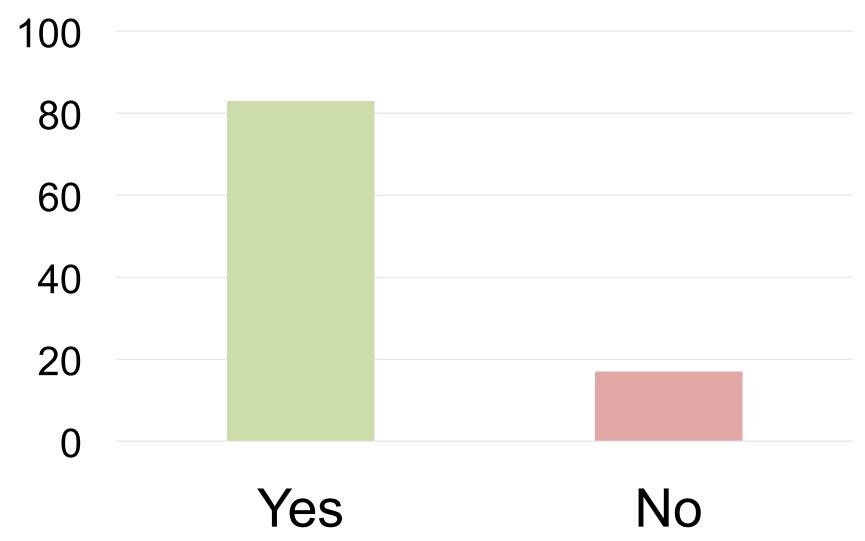


### Loading...





### Instant Results





# What makes your native language more complex than English?



### More Morphological Variants = A More Complex Language

 I agree: a lot of morphological variants can make a language "difficult":

Mark Twain said it best: "I'd rather decline two

drinks than one German adjective."

Then, look at how simple English is!

- Your average verb has four inflections:
   run, runs, ran, running
- Nouns and adjectives don't inflect in English according to case
  - The adjective good has one inflection



### In Comparison: The Turkish Verb

- koşmak = Turkish verb "to run"
  - (partial) paradigm  $\rightarrow$
- Tense, mood, evidentiality ... marked through morphology
  - 100+ forms in Turkish!
- Archi (Kibrik 1998) has 1.5 million verb forms
  - It's very, very agglutinative
- This makes a language more complex!

ben koşıyorum sen koşıyorsun

o koşıyor

biz koşıyoruz

siz koşıyorsunuz

onlar koşıyorlar

ben koşmadın sen koşmadın o koşmadı

biz koşmadık

siz koşmadınız

onlar koşmadılar



# Number of Forms is Only One Dimension of Morphological Complexity

- There are (at least) two types of morphological complexity
  - Type 1: how big are the paradigms? (seen before)
  - Type 2: how irregular are the paradigms?

- Ackerman and Malouf (2013) introduce the technical jargon
  - Enumerative Complexity (E-Complexity)
  - Integrative Complexity (I-Complexity)



### English versus Turkish: # Forms

- English
  - 4 verbal slots
  - 2 nominal slots
  - 1 adjectival slot
    - 7 Total
- Turkish is more morphologically complex under # forms per verb

- Turkish
  - 350 verbal slots
  - 8 nominal slots
  - 1 adjectival slots

358 Total



### English Versus Turkish: Irregularity

#### English

- 224 irregular verbs
- 10 irregular nouns
- 0 irregular adjectives

#### Turkish

- 1 irregular verb
- 0 irregular nouns
- 0 irregular adjectives

234 Total

1 Total

English is more morphologically complex under amount of irregularity



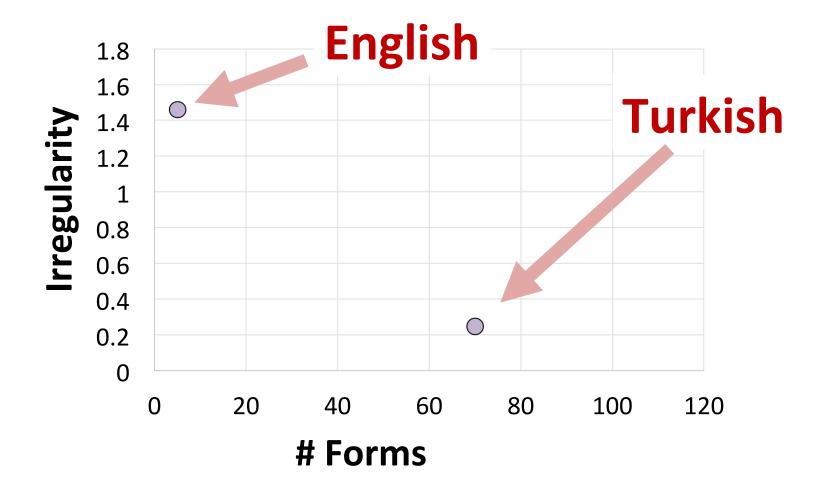
### What's *This* Paper About?

### Good Linguistic Question:

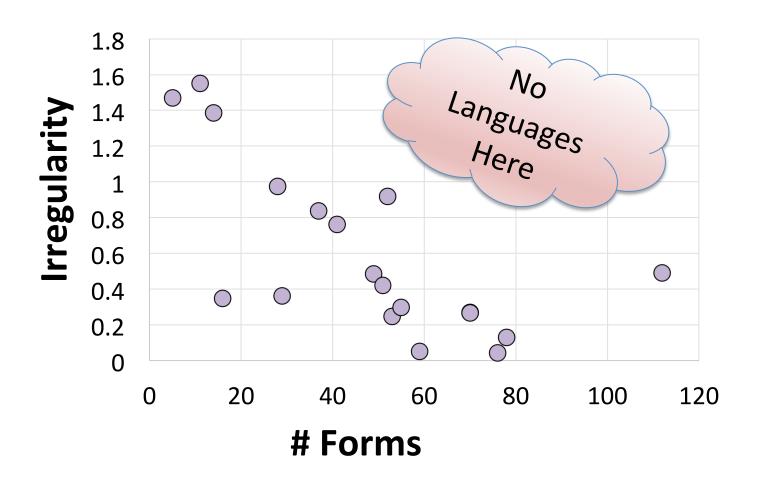
How do the # morphological variants and morphological irregularity interact?



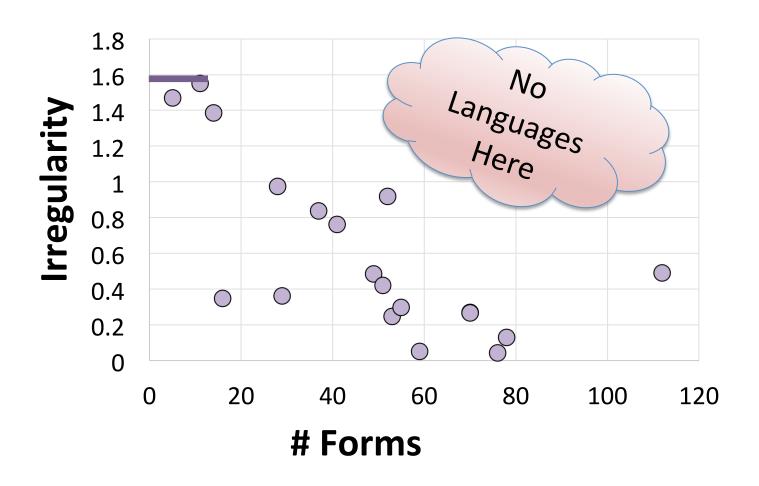
### Plotting English and Turkish Verbs



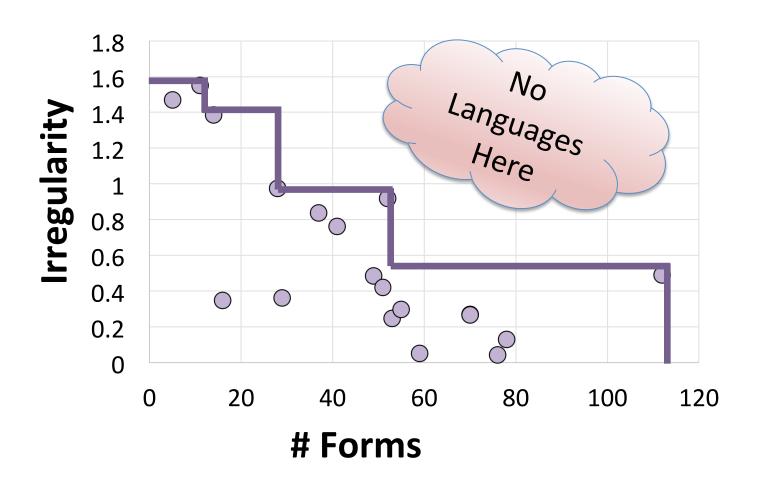






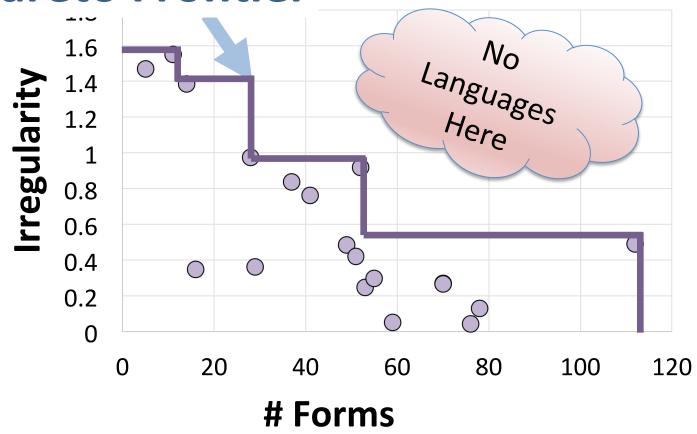






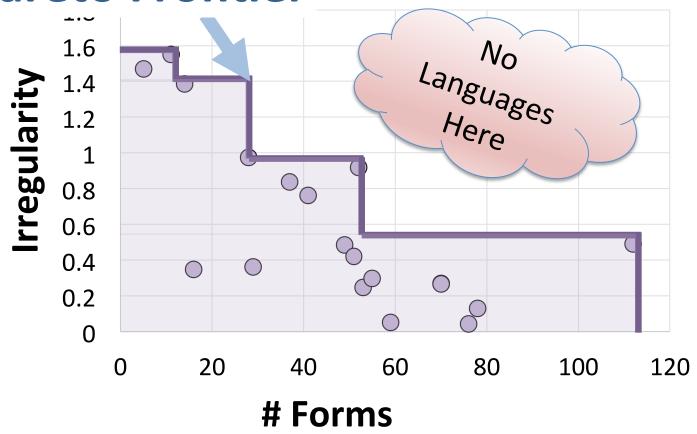


**Pareto Frontier** 





**Pareto Frontier** 





### Scientific Hypothesis about Language

 Use machine learning techniques to test hypothesis about Language

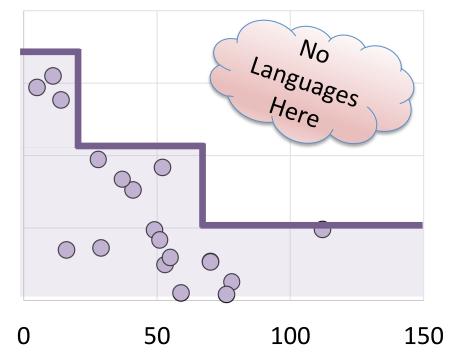
1.5

 Morphological systems can have either a lot of forms or 1 lot of irregularity

– But not both!

0.5

 Why? Speculative reason: memorizing a lot of irregulars would tax human memory





# Chinese is Low on *Both* Dimensions of Morphological Complexity

- Morphology in a language is not necessary!
- Let's look at the Chinese verb "to drink"
  - drink = 喝
  - drinking = 喝
  - drank = 喝

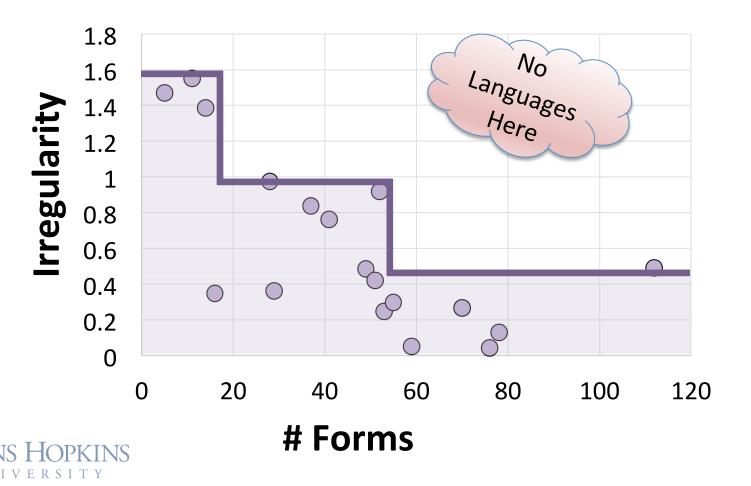


Look mommy, no inflection!



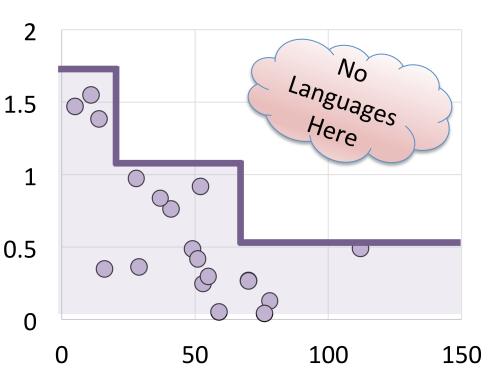
### Our Hypothesis Again

 Inflectional, morphological systems have a lot of forms, or a lot irregularity, but not both



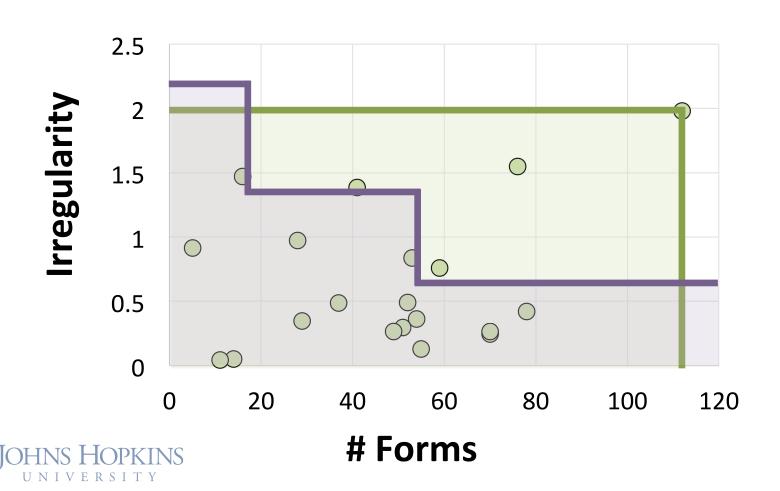
#### A Paired Permutation Test

- There appears to be a trend, but is it significant?
  - Is the upper right-hand corner more empty that it would be by chance?
- New Significance Test
  - Keep x-axis in tact, shuffle y-axis
  - compare area under the Pareto curve
  - Non-parametric test

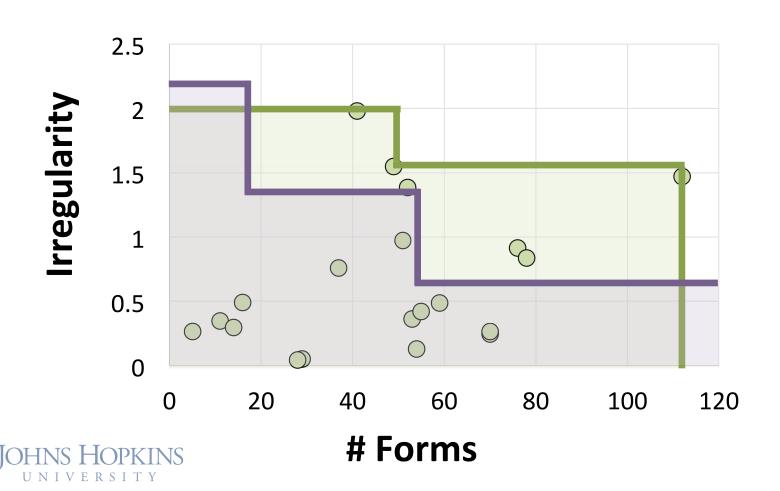




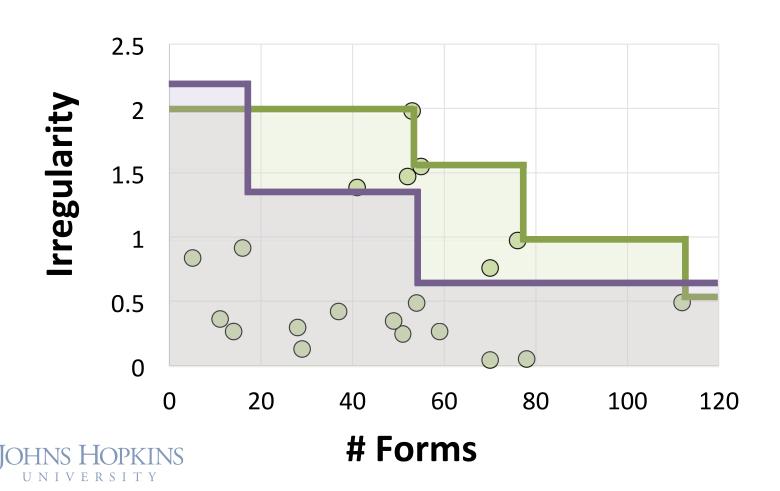
### Random Morphological Trade-Off



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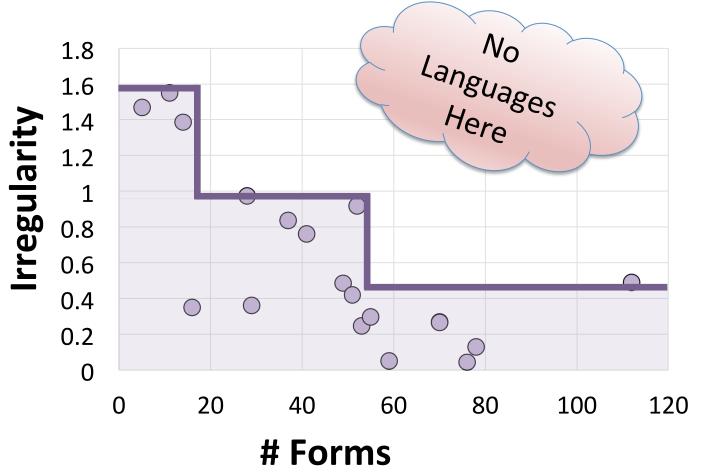


### Random Morphological Trade-Off



### Scientific Finding

Gap in the upper right-hand size with p < 0.05





### Caution: Limited # Of Languages

- We need to be very cautious about reporting the results!
- The languages are not i.i.d.
  - Some of them are genetically related
  - Focus on Western European Languages
- We have a small sample of size of languages
  - There might be unobserved counterexamples
  - For this sample, the Pareto frontier leaves an unusually large gap in the upper right

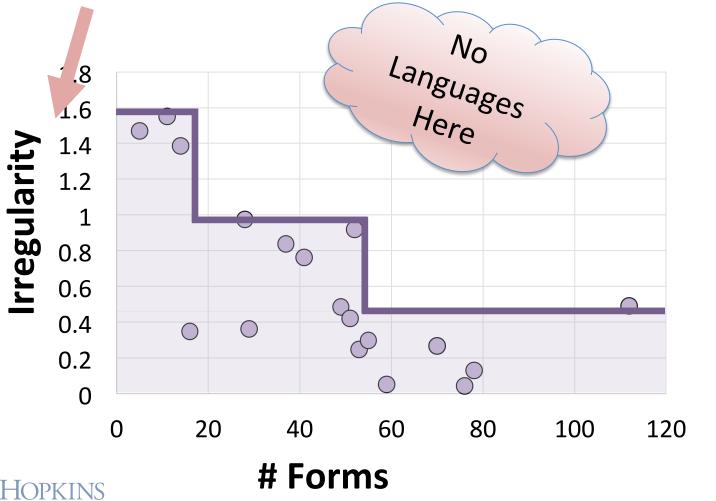


# Technical Contribution: Operationalizing Morphological Irregularity



### Where did the y-axis come from?

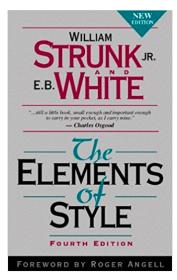
What do those numbers mean?





### What's an Irregular Verb?

- TL;DR: some grammarian said so
- **Example:** Spanish has three types of regular verbs
  - ar, er, ir
- The rest are "irregular"
  - Why???
- Are they equally irregular?
  - Or are some verbs more irregular than others?



| CANTAR      | BEBER      | VIVIR      |
|-------------|------------|------------|
| cant-é      | beb-í      | viv-í      |
| cant-aste   | beb-iste   | viv-iste   |
| cant-ó      | beb-ió     | viv-ió     |
| cant-amos   | beb-imos   | viv-imos   |
| cant-asteis | beb-isteis | viv-isteis |
| cant-aron   | beb-ieron  | viv-ieron  |



# New Insight: We will tackle morphological irregularity probabilistically



### Regularity = Predictability

- For each language
  - Step 1: Build a really good generative probability model p of the morphological paradigm

Step 2: Train its parameters on some data

- Step 3: Irregularity =  $-\log p(\text{held-out data})$ 



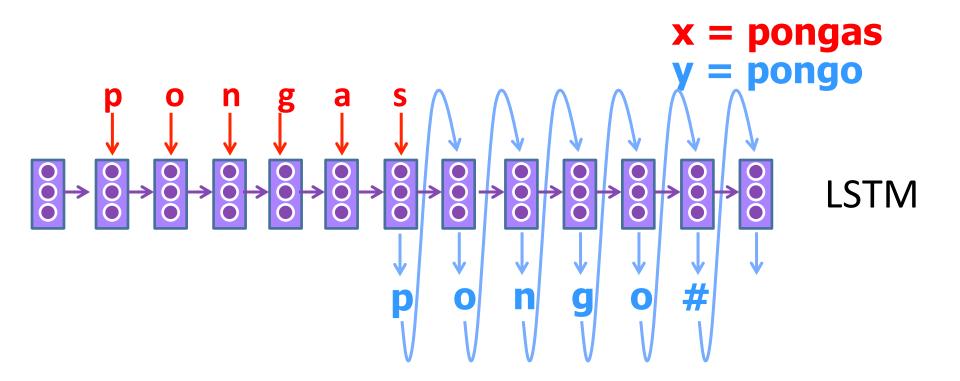
### Morphological Reinflection

Start with pair-wise probability distributions

- In NLP, this task is known as morphological reinflection
  - Three shared tasks: SIGMORPHON (2016), CoNLL (2017, 2018)
  - Cotterell et al. (2016,2017) for overview of the results
  - State of the art: LSTM seq2seq model same as MT



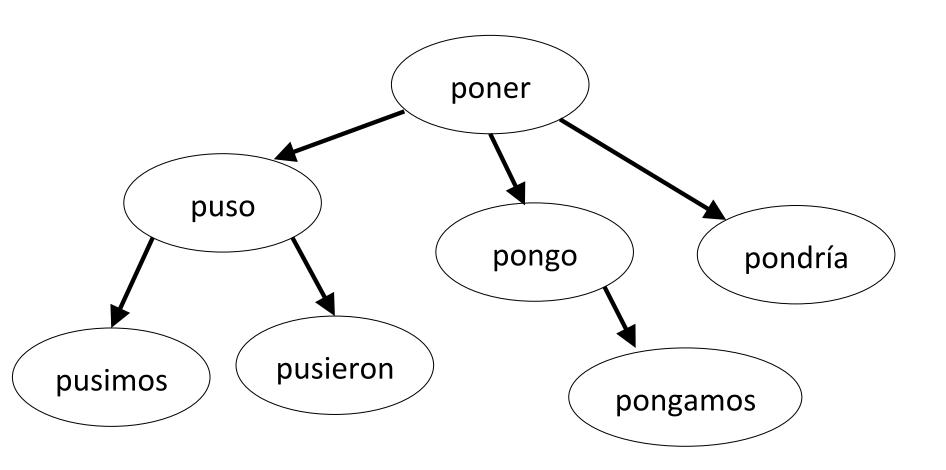
### Sequence-to-Sequence Model



p(y | x) reads x, then stochastically emits chars of y, 1 by 1, like a language model

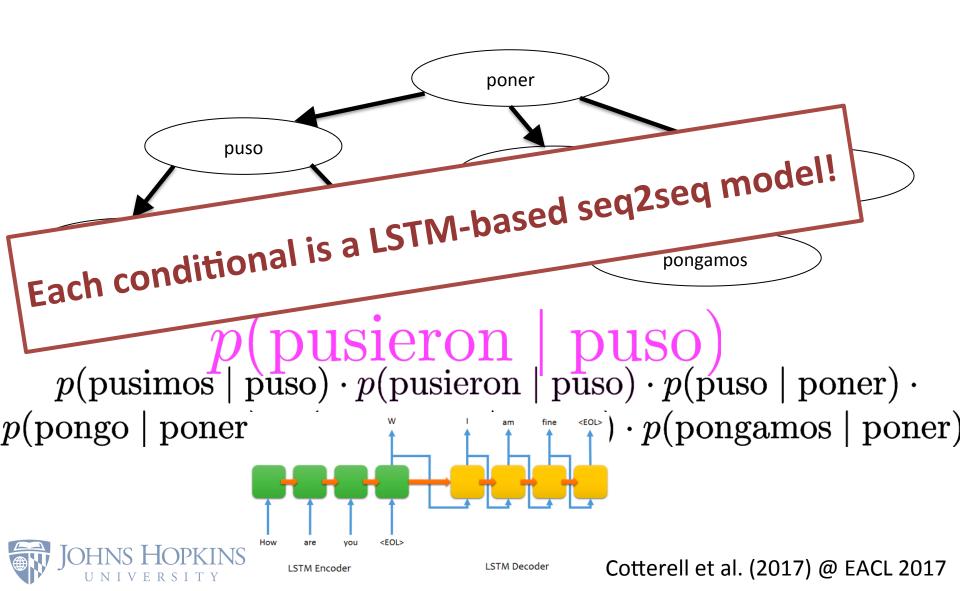


### Arrange into a Bayesian Network

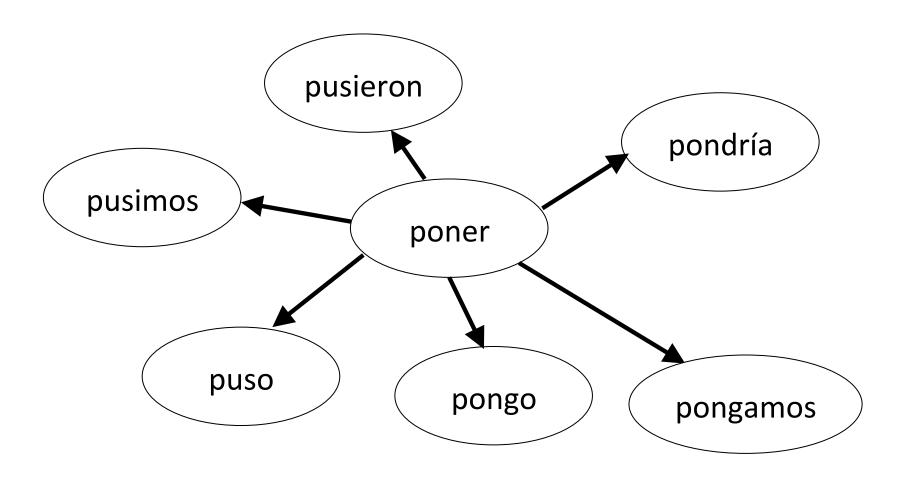




# Neural Graphical Model Over Strings



## Many Possible Networks





#### How to Choose Best Tree?

Standard structure learning problem in graphical models

- Strategy: Tie parameters among all conditionals
  - Conditionals for every possible tree trained together
- Inspired by Chow-Liu Algorithm
  - Use Chu-Liu-Edmonds
  - Finds optimal directed spanning tree in  $O(n^3)$  time



## Experimental Languages

#### **Cross-linguistically Compatible Labels**

- Data from the UniMorph (Kirov et al. 2018)
- Selected languages with "enough" training examples
- Verbal Paradigms:
  - 23 languages / 3 families
- Nominal Paradigms
  - 31 languages / 3 families

```
Akademie
             Akademie
                          N; ACC; SG
                          VADAT; SG
Akademie
             Akademie
                             EN:SG
Akademie
             Akademie
Akademie
             Akademien
                          N; ACC; PL
Akademie
             Akademien
                          N; DAT; PL
             Akademien
Akademie
                          N; GEN; PL
Akademie
             Akademien
                          N; NOM; PL
Akademie
             Akademie
                          N; NOM; SG
Akademiker
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Akademiker
             Akademiker
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             Akademiker
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Akademiker
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Akademiker
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Akademiker
             Akademiker
                          N; NOM; PL
Akademiker
             Akademiker
                          N:NOM:SG
Akademiker
             Akademikers N; GEN; SG
```



## Plug For UniMorph

Now data for over 100 languages!

Freely downloadable from unimorph.github.io



Schema

Software

Publications

Contact

#### UniMorph

The Universal Morphology (UniMorph) project is a collaborative effort to improve how NLP handles complex morphology in the world's languages. The goal of UniMorph is to annotate morphological data in a universal schema that allows an inflected word from any language to be defined by its lexical meaning, typically carried by the lemma, and by a rendering of its inflectional form in terms of a bundle of morphological features from our schema. The specification of the schema is described here and in Sylak-Glassman (2016).



#### Estimating the Parameters

 Estimating morphological irregularity is now a standard machine learning problem

- Model is trained using gradient descent on UniMorph data
  - Best model selected on development data

Irregularity = loss on held-out data



#### But why is there a trade-off?

- This paper shows the existence of a trade-off between two types of morphological complexity
- The real scientific question is why?
- On-going work guesses that it has to learnability and the learning infrequent, irregular forms
  - I.e., rare forms tend to regularize
- Artificial learnability study already available
  - Preliminary version on arXiv



## Linguistic Complexity More Broadly



## A Twitter Poll About Complexity



Do you think your native language is more complex than English? (If you speak a language other than English natively.) #acl2018

Also, come to my talk at 17:00 tomorrow @acl2018 on that very topic!

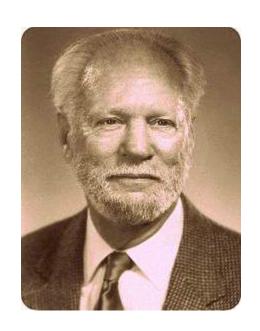
**79**% Yes

21% No

109 votes • 1 day left



## Equal Complexity Hypothesis



 Hockett (1958) argued that all languages are equally complex

 Idea goes back much further in the linguistics literature

 All languages appear to optimize for efficient communication subject to learnability



## Complexity Trade-Offs

 Corollary: if one facet of a language is more complex, another is simpler to compensate

#### Trade-Off Example:

- German has more inflected forms than English (morphology)
- English has a more complicated tense system (syntax)





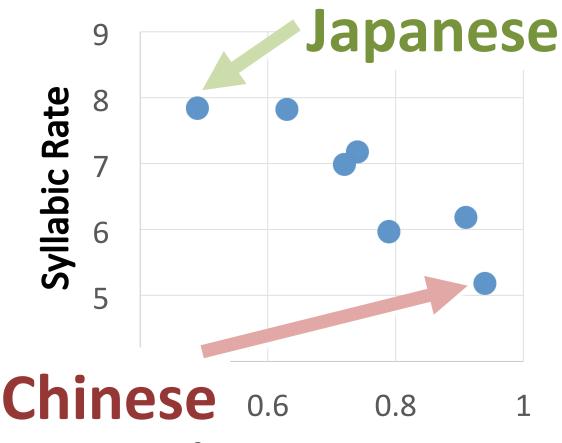
#### Example: Rate Of Speech (Pellegrino 2011)

Are all languages spoken equally fast?

No!

- Spoken Rapidly
  - Spanish, Japanese

- Spoken Slowly
  - English, Chinese





**Information Density** 

#### John McWhorter on Creoles

- McWhorter wrote the seminal paper in 2001
- Argues creoles are in fact less complex
- Complexity accretes over time
  - Creoles are new languages





#### Published Work

• Check out our NAACL 2018 paper: *All Are Languages Equally Hard to Language-Model?* 



#### Future Work

- We only looked a specific trade-off in morphological complexity
  - Data-driven methods for trade-offs in other areas of linguistics
- Extensions look at language more holistically
  - Trade-offs between morphology and phonology
  - Trade-offs between morphology and syntax
- Why didn't linguistics already solve this problem?
  - No big data, no methods



## Fin

